

Name_____

ABSOLUTE VALUE INEQUALITIES #1

Directions: Solving *absolute value inequalities* requires two different strategies. To solve absolute value inequalities with a “greater than” symbol, you should split the problem into two separate inequalities, like solving an absolute value equation. This strategy is demonstrated in Example 1. For inequalities with a “less than” symbol, you can solve the two inequalities at the same time, as shown in Example 2.

Example 1:

$|x + 7| > 10$

$x + 7 < -10$
 $x < -17$

or

$x + 7 > 10$
 $x > 3$

(subtract 7 from both sides)

$|x + 4| < 10$

$-10 < x + 4 < 10$
 $-14 < x < 6$

(subtract 4 from each part)

1) $|x + 8| < 13$

2) $|x - 8| > 22$

3) $|x + 2| \leq 8$

4) $|10 + x| < 14$

5) $|x - 20| \geq 42$

6) $|x + 2| < 20$

7) $|x + 10| \leq 20$

8) $|x - 2| > 12$

9) $|2 + x| < 24$

Name _____

ABSOLUTE VALUE INEQUALITIES #1--KEY

Directions: Solving *absolute value inequalities* requires two different strategies. To solve absolute value inequalities with a “greater than” symbol, you should split the problem into two separate inequalities, like solving an absolute value equation. This strategy is demonstrated in Example 1. For inequalities with a “less than” symbol, you can solve the two inequalities at the same time, as shown in Example 2.

Example 1: $|x + 7| > 10$

$$\begin{array}{lcl} x + 7 < -10 & \text{or} & x + 7 > 10 \quad (\text{subtract 7 from both sides}) \\ x < -17 & \text{or} & x > 3 \end{array}$$

$|x + 4| < 10$

$$\begin{array}{l} -10 < x + 4 < 10 \quad (\text{subtract 4 from each part}) \\ -14 < x < 6 \end{array}$$

1) $|x + 8| < 13$

2) $|x - 8| > 22$

3) $|x + 2| \leq 8$

$-21 < x < 5$

$x < -14$ **or** $x > 30$

$-10 \leq x \leq 6$

4) $|10 + x| < 14$

5) $|x - 20| \geq 42$

6) $|x + 2| < 20$

$-24 < x < 4$

$x \leq -22$ **or** $x \geq 62$

$-22 < x < 18$

7) $|x + 10| \leq 20$

8) $|x - 2| > 12$

9) $|2 + x| < 24$

$-30 \leq x \leq 10$

$x < -10$ **or** $x > 14$

$-26 < x < 22$